

Appendix F

Examination of Alternative Procedures

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Examination of Alternative Procedures

F.1 Alternative Procedure (Baysian Approach) for Determining Population Distribution

To study the effect of incorporating into the analysis the uncertainty associated with the unknown population distribution, one must consider the parameters of any probability distribution as random variables. After selection of the parametric distribution (e.g., lognormal, Weibull, etc.) that best fits the data, one can incorporate the uncertainty of the distribution by randomly drawing parameter values from suitable parameter distributions. The selection usually depends on previous information. In this application, it was assumed that a sensible parameter distribution was the uniform distribution; in other words, a parameter will be drawn randomly from intervals centered in the maximum likelihood parameter estimate, and end points equal to the maximum likelihood estimator plus/minus its standard error.

The construction of the hypothetical distribution (e.g., a hypothetical Weibull distribution) proceeded as follows:

1. Draw one set of model parameters (shape and scale parameters) at random from the corresponding intervals.
2. Perform a goodness-of-fit test to assess if the data (e.g., carbon monoxide) came from the distribution (e.g., Weibull) with the parameters selected.
3. If the p-value of the goodness-of-fit test statistic is larger than 0.40, then one value is randomly selected from this distribution (e.g., Weibull). If the p-value is lower than 0.40, the set of parameters are discarded, and steps 1 and 2 are repeated.

This process is repeated 10,000 times to obtain a hypothetical distribution that will account for the uncertainty associated with the unknown distribution. Once the hypothetical distribution is obtained, the adjustments are calculated following steps 5-7 of the statistical analysis presented in Section 3.2.

This process was applied to three emissions factors to assess the effect of the uncertainty of the distribution on the calculation of the adjustments. Two emissions factors with high p-values on the goodness-of-fit test were selected, which were Wood Combustion Formaldehyde ($p = 0.9245$), and Wood Combustion Carbon Monoxide ($p = 0.904$), and one with low p-values, which was Wood Combustion Nitrogen Oxides ($p=0.137$).

Table F-1 compares the uncertainty ratios calculated by the alternative approach to the values reported in the study, using the Baysian approach, for the 90th percentile and mean target statistics. Tables F-2 through F-4 report all of the calculated uncertainty ratios for formaldehyde, carbon monoxide, and nitrogen oxides, respectively. Tables F-2a through F-4a present the uncertainty ratios reported in the study for these same pollutants, respectively. The uncertainty ratios calculated using the alternative approach show a greater range for most of the pollutants examined. However, some reduction of the uncertainty ratios were observed for percentiles above the mean for nitrogen oxides, especially for the smaller sample size. Further research is needed to account for variability for those pollutants with lower goodness-of-fit test p-values.

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Table F-1 Comparison of Selected Emission Factor Uncertainty Ratios Calculated Using Original (Frequentist) and Modified (Baysian) Approach

| Pollutant | n-value | Adjustment (Monte Carlo Median Value) | | | |
|--------------|---------|---|--------------------------------------|---|--------------------------------------|
| | | Target Statistic: 90th Percentile | | Target Statistic: Mean | |
| | | Original Reported Value (Frequentist) | Alternative Approach (Baysian) | Original Reported Value (Frequentist) | Alternative Approach (Baysian) |
| Formaldehyde | 1 | 11.18 | 11.59 | 5.79 | 6.65 |
| | 3 | 5.23 | 5.21 | 2.71 | 2.99 |
| | 5 | 4.08 | 4.09 | 2.12 | 2.35 |
| | 10 | 3.15 | 3.20 | 1.63 | 1.83 |
| | 15 | 2.88 | 2.91 | 1.49 | 1.67 |
| | 20 | 2.73 | 2.60 | 1.41 | 1.49 |
| | 25 | 2.63 | 2.53 | 1.36 | 1.45 |
| CO | 1 | 2.22 | 2.41 | 1.16 | 1.19 |
| | 3 | 1.97 | 2.24 | 1.04 | 1.11 |
| | 5 | 1.94 | 2.11 | 1.02 | 1.04 |
| | 10 | 1.92 | 2.04 | 1.01 | 1.01 |
| | 15 | 1.92 | 2.08 | 1.01 | 1.03 |
| | 20 | 1.92 | 2.03 | 1.01 | 1.00 |
| | 25 | 1.91 | 2.06 | 1.00 | 1.02 |
| NOx | 1 | 4.92 | 1.92 | 2.16 | 1.14 |
| | 3 | 3.27 | 1.79 | 1.44 | 1.06 |
| | 5 | 2.93 | 1.72 | 1.29 | 1.02 |
| | 10 | 2.61 | 1.71 | 1.15 | 1.01 |
| | 15 | 2.56 | 1.70 | 1.12 | 1.01 |
| | 20 | 2.48 | 1.69 | 1.09 | 1.00 |
| | 25 | 2.45 | 1.70 | 1.08 | 1.01 |

Table F-2. Alternative (Bayesian) Approach: Emissions Factor Uncertainty Ratios by Number of Tests (n) and Target Statistic: Wood Residue Combustion, Formaldehyde

| | | Target Statistic | | | | | | | | | | | | | | | |
|----------------------|--|------------------|--------------|--------------|---------------|---------------|---------------|---------------|---------|----------|---------------|---------------|---------------|---------------|---------------|---------------|------------|
| Median | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | | 0.0006 | 0.0147 | 0.0465 | 0.0945 | 0.1497 | 0.2148 | 0.2934 | 1.0409 | 6.6505 | 3.5814 | 4.9244 | 7.1432 | 11.5950 | 21.7888 | 99.2299 | 1556.0021 |
| 3 | | 0.0003 | 0.0066 | 0.0209 | 0.0424 | 0.0672 | 0.0965 | 0.1318 | 0.4675 | 2.9869 | 1.6085 | 2.2117 | 3.2082 | 5.2076 | 9.7858 | 44.5664 | 698.8360 |
| 5 | | 0.0002 | 0.0052 | 0.0164 | 0.0333 | 0.0528 | 0.0758 | 0.1035 | 0.3671 | 2.3456 | 1.2631 | 1.7368 | 2.5193 | 4.0894 | 7.6846 | 34.9972 | 548.7824 |
| 10 | | 0.0002 | 0.0041 | 0.0128 | 0.0260 | 0.0413 | 0.0592 | 0.0809 | 0.2870 | 1.8338 | 0.9875 | 1.3578 | 1.9696 | 3.1971 | 6.0079 | 27.3610 | 429.0418 |
| 15 | | 0.0001 | 0.0037 | 0.0117 | 0.0237 | 0.0376 | 0.0540 | 0.0737 | 0.2615 | 1.6706 | 0.8997 | 1.2370 | 1.7944 | 2.9127 | 5.4734 | 24.9268 | 390.8715 |
| 20 | | 0.0001 | 0.0033 | 0.0104 | 0.0211 | 0.0335 | 0.0481 | 0.0657 | 0.2330 | 1.4885 | 0.8016 | 1.1022 | 1.5988 | 2.5952 | 4.8768 | 22.2099 | 348.2690 |
| 25 | | 0.0001 | 0.0032 | 0.0101 | 0.0206 | 0.0327 | 0.0469 | 0.0640 | 0.2271 | 1.4510 | 0.7814 | 1.0744 | 1.5585 | 2.5299 | 4.7540 | 21.6506 | 339.4979 |
| Mean | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | | 0.0030 | 0.0734 | 0.2316 | 0.4704 | 0.7454 | 1.0698 | 1.4608 | 5.1836 | 33.1178 | 17.8345 | 24.5222 | 35.5712 | 57.7398 | 108.5023 | 494.1384 | 7748.4719 |
| 3 | | 0.0006 | 0.0140 | 0.0443 | 0.0900 | 0.1426 | 0.2047 | 0.2795 | 0.9919 | 6.3375 | 3.4128 | 4.6926 | 6.8070 | 11.0492 | 20.7632 | 94.5592 | 1482.7611 |
| 5 | | 0.0003 | 0.0084 | 0.0266 | 0.0541 | 0.0857 | 0.1231 | 0.1680 | 0.5963 | 3.8098 | 2.0516 | 2.8210 | 4.0920 | 6.6422 | 12.4818 | 56.8441 | 891.3599 |
| 10 | | 0.0002 | 0.0054 | 0.0170 | 0.0346 | 0.0549 | 0.0787 | 0.1075 | 0.3815 | 2.4376 | 1.3127 | 1.8049 | 2.6182 | 4.2498 | 7.9861 | 36.3702 | 570.3135 |
| 15 | | 0.0002 | 0.0045 | 0.0141 | 0.0286 | 0.0454 | 0.0651 | 0.0889 | 0.3155 | 2.0157 | 1.0855 | 1.4925 | 2.1650 | 3.5143 | 6.6039 | 30.0752 | 471.6026 |
| 20 | | 0.0002 | 0.0039 | 0.0124 | 0.0251 | 0.0398 | 0.0571 | 0.0780 | 0.2768 | 1.7687 | 0.9525 | 1.3096 | 1.8997 | 3.0836 | 5.7946 | 26.3896 | 413.8088 |
| 25 | | 0.0001 | 0.0037 | 0.0116 | 0.0235 | 0.0373 | 0.0535 | 0.0730 | 0.2591 | 1.6554 | 0.8915 | 1.2258 | 1.7781 | 2.8862 | 5.4236 | 24.7000 | 387.3156 |
| 95 Percentile | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | | 0.0127 | 0.3144 | 0.9923 | 2.0154 | 3.1936 | 4.5834 | 6.2587 | 22.2085 | 141.8894 | 76.4099 | 105.0625 | 152.4008 | 247.3799 | 464.8658 | 2117.0808 | 33197.4647 |
| 3 | | 0.0021 | 0.0510 | 0.1610 | 0.3270 | 0.5181 | 0.7435 | 1.0153 | 3.6028 | 23.0184 | 12.3958 | 17.0440 | 24.7236 | 40.1318 | 75.4141 | 343.4489 | 5385.5445 |
| 5 | | 0.0011 | 0.0269 | 0.0850 | 0.1726 | 0.2735 | 0.3925 | 0.5359 | 1.9017 | 12.1501 | 6.5430 | 8.9966 | 13.0502 | 21.1833 | 39.8067 | 181.2868 | 2842.7167 |
| 10 | | 0.0006 | 0.0145 | 0.0458 | 0.0930 | 0.1474 | 0.2116 | 0.2889 | 1.0253 | 6.5503 | 3.5275 | 4.8502 | 7.0356 | 11.4203 | 21.4606 | 97.7352 | 1532.5638 |
| 15 | | 0.0004 | 0.0108 | 0.0340 | 0.0691 | 0.1095 | 0.1572 | 0.2147 | 0.7618 | 4.8671 | 2.6210 | 3.6038 | 5.2276 | 8.4856 | 15.9457 | 72.6195 | 1138.7303 |
| 20 | | 0.0004 | 0.0091 | 0.0286 | 0.0580 | 0.0919 | 0.1320 | 0.1802 | 0.6394 | 4.0852 | 2.2000 | 3.0249 | 4.3878 | 7.1224 | 13.3842 | 60.9539 | 955.8044 |
| 25 | | 0.0003 | 0.0080 | 0.0251 | 0.0510 | 0.0808 | 0.1160 | 0.1583 | 0.5619 | 3.5897 | 1.9331 | 2.6580 | 3.8557 | 6.2586 | 11.7609 | 53.5611 | 839.8801 |

Table F-2a (Also Table D.1-7). Frequentist Approach: Emissions Factor Uncertainty Ratios by Number of Tests (n) and Target Statistic: Wood Residue Combustion, Formaldehyde, Uncontrolled

| Target Statistics | | | | | | | | | | | | | | | | |
|----------------------|---------|--------------|--------------|---------------|---------------|---------------|---------------|---------|----------|---------------|---------------|---------------|---------------|---------------|---------------|------------|
| Median | | | | | | | | | | | | | | | | |
| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| 1 | 0.0010 | 0.0141 | 0.0468 | 0.0923 | 0.1440 | 0.2102 | 0.2874 | 0.9697 | 5.7927 | 3.4813 | 4.7639 | 6.9925 | 11.1801 | 21.5015 | 78.4189 | 1724.1519 |
| 3 | 0.0005 | 0.0066 | 0.0219 | 0.0432 | 0.0674 | 0.0983 | 0.1345 | 0.4537 | 2.7101 | 1.6287 | 2.2288 | 3.2715 | 5.2307 | 10.0595 | 36.6885 | 806.6495 |
| 5 | 0.0004 | 0.0052 | 0.0171 | 0.0337 | 0.0526 | 0.0768 | 0.1050 | 0.3541 | 2.1154 | 1.2713 | 1.7397 | 2.5535 | 4.0827 | 7.8519 | 28.6369 | 629.6239 |
| 10 | 0.0003 | 0.0040 | 0.0132 | 0.0260 | 0.0405 | 0.0592 | 0.0809 | 0.2730 | 1.6311 | 0.9803 | 1.3414 | 1.9689 | 3.1481 | 6.0543 | 22.0809 | 485.4802 |
| 15 | 0.0003 | 0.0036 | 0.0120 | 0.0238 | 0.0371 | 0.0541 | 0.0740 | 0.2497 | 1.4915 | 0.8964 | 1.2266 | 1.8004 | 2.8786 | 5.5362 | 20.1912 | 443.9329 |
| 20 | 0.0002 | 0.0034 | 0.0114 | 0.0225 | 0.0351 | 0.0513 | 0.0702 | 0.2367 | 1.4139 | 0.8497 | 1.1628 | 1.7067 | 2.7289 | 5.2481 | 19.1407 | 420.8347 |
| 25 | 0.0002 | 0.0033 | 0.0110 | 0.0217 | 0.0339 | 0.0495 | 0.0677 | 0.2284 | 1.3645 | 0.8200 | 1.1221 | 1.6471 | 2.6335 | 5.0647 | 18.4716 | 406.1250 |
| Mean | | | | | | | | | | | | | | | | |
| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| 1 | 0.0052 | 0.0745 | 0.2465 | 0.4868 | 0.7593 | 1.1083 | 1.5158 | 5.1133 | 30.5463 | 18.3579 | 25.1210 | 36.8731 | 58.9557 | 113.3829 | 413.5232 | 9091.8965 |
| 3 | 0.0009 | 0.0134 | 0.0442 | 0.0873 | 0.1362 | 0.1989 | 0.2720 | 0.9175 | 5.4808 | 3.2939 | 4.5074 | 6.6161 | 10.5783 | 20.3440 | 74.1974 | 1631.3357 |
| 5 | 0.0006 | 0.0084 | 0.0279 | 0.0551 | 0.0859 | 0.1254 | 0.1715 | 0.5785 | 3.4559 | 2.0770 | 2.8421 | 4.1717 | 6.6701 | 12.8278 | 46.7847 | 1028.6278 |
| 10 | 0.0004 | 0.0053 | 0.0174 | 0.0344 | 0.0537 | 0.0783 | 0.1071 | 0.3614 | 2.1591 | 1.2976 | 1.7756 | 2.6063 | 4.1671 | 8.0141 | 29.2287 | 642.6343 |
| 15 | 0.0003 | 0.0045 | 0.0148 | 0.0292 | 0.0455 | 0.0664 | 0.0908 | 0.3064 | 1.8303 | 1.1000 | 1.5052 | 2.2094 | 3.5326 | 6.7939 | 24.7782 | 544.7840 |
| 20 | 0.0003 | 0.0040 | 0.0134 | 0.0264 | 0.0412 | 0.0602 | 0.0823 | 0.2776 | 1.6582 | 0.9966 | 1.3637 | 2.0017 | 3.2004 | 6.1551 | 22.4483 | 493.5585 |
| 25 | 0.0003 | 0.0038 | 0.0125 | 0.0246 | 0.0384 | 0.0561 | 0.0767 | 0.2589 | 1.5465 | 0.9294 | 1.2718 | 1.8668 | 2.9848 | 5.7404 | 20.9360 | 460.3089 |
| 95 Percentile | | | | | | | | | | | | | | | | |
| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| 1 | 0.0201 | 0.2899 | 0.9593 | 1.8941 | 2.9545 | 4.3124 | 5.8978 | 19.8958 | 118.8548 | 71.4301 | 97.7452 | 143.4723 | 229.3949 | 441.1696 | 1609.0062 | 35376.2962 |
| 3 | 0.0033 | 0.0471 | 0.1557 | 0.3074 | 0.4796 | 0.7000 | 0.9573 | 3.2295 | 19.2927 | 11.5947 | 15.8662 | 23.2887 | 37.2358 | 71.6114 | 261.1768 | 5742.3447 |
| 5 | 0.0019 | 0.0268 | 0.0886 | 0.1749 | 0.2728 | 0.3982 | 0.5447 | 1.8374 | 10.9761 | 6.5965 | 9.0266 | 13.2495 | 21.1843 | 40.7414 | 148.5896 | 3266.9553 |
| 10 | 0.0010 | 0.0140 | 0.0463 | 0.0914 | 0.1426 | 0.2081 | 0.2846 | 0.9601 | 5.7354 | 3.4469 | 4.7168 | 6.9233 | 11.0696 | 21.2889 | 77.6435 | 1707.1033 |
| 15 | 0.0007 | 0.0108 | 0.0358 | 0.0706 | 0.1101 | 0.1608 | 0.2199 | 0.7417 | 4.4308 | 2.6628 | 3.6439 | 5.3485 | 8.5516 | 16.4464 | 59.9823 | 1318.7953 |
| 20 | 0.0006 | 0.0092 | 0.0304 | 0.0601 | 0.0937 | 0.1368 | 0.1871 | 0.6313 | 3.7713 | 2.2665 | 3.1015 | 4.5524 | 7.2787 | 13.9983 | 51.0537 | 1122.4879 |
| 25 | 0.0006 | 0.0080 | 0.0263 | 0.0520 | 0.0811 | 0.1184 | 0.1619 | 0.5463 | 3.2634 | 1.9613 | 2.6838 | 3.9394 | 6.2986 | 12.1133 | 44.1789 | 971.3371 |

Table F-3. Alternative (Bayesian) Approach: Emissions Factor Uncertainty Ratios by Number of Tests (n) and Target Statistic: Wood Residue Combustion, CO

| | | Target Statistic | | | | | | | | | | | | | | | |
|----------------------|--|------------------|--------------|--------------|---------------|---------------|---------------|---------------|--------|--------|---------------|---------------|---------------|---------------|---------------|---------------|---------|
| Median | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | | 0.010 | 0.029 | 0.106 | 0.183 | 0.290 | 0.431 | 0.512 | 0.953 | 1.190 | 1.653 | 1.874 | 2.100 | 2.408 | 2.872 | 4.427 | 6.538 |
| 3 | | 0.010 | 0.027 | 0.099 | 0.171 | 0.270 | 0.402 | 0.477 | 0.887 | 1.108 | 1.540 | 1.745 | 1.955 | 2.243 | 2.674 | 4.123 | 6.088 |
| 5 | | 0.009 | 0.026 | 0.093 | 0.161 | 0.255 | 0.378 | 0.449 | 0.836 | 1.044 | 1.451 | 1.644 | 1.842 | 2.113 | 2.519 | 3.884 | 5.736 |
| 10 | | 0.009 | 0.025 | 0.090 | 0.155 | 0.246 | 0.365 | 0.433 | 0.806 | 1.007 | 1.399 | 1.586 | 1.777 | 2.038 | 2.430 | 3.746 | 5.532 |
| 15 | | 0.009 | 0.025 | 0.092 | 0.158 | 0.251 | 0.373 | 0.443 | 0.824 | 1.029 | 1.430 | 1.621 | 1.816 | 2.084 | 2.484 | 3.830 | 5.656 |
| 20 | | 0.009 | 0.025 | 0.090 | 0.155 | 0.245 | 0.364 | 0.433 | 0.805 | 1.004 | 1.396 | 1.582 | 1.773 | 2.033 | 2.425 | 3.738 | 5.520 |
| 25 | | 0.009 | 0.025 | 0.091 | 0.157 | 0.248 | 0.369 | 0.439 | 0.816 | 1.018 | 1.415 | 1.604 | 1.798 | 2.062 | 2.458 | 3.790 | 5.597 |
| Mean | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | | 0.032 | 0.094 | 0.338 | 0.583 | 0.923 | 1.372 | 1.630 | 3.032 | 3.785 | 5.261 | 5.964 | 6.681 | 7.664 | 9.138 | 14.087 | 20.803 |
| 3 | | 0.011 | 0.032 | 0.117 | 0.201 | 0.319 | 0.474 | 0.563 | 1.047 | 1.307 | 1.816 | 2.059 | 2.306 | 2.646 | 3.154 | 4.863 | 7.182 |
| 5 | | 0.010 | 0.029 | 0.104 | 0.180 | 0.285 | 0.424 | 0.503 | 0.936 | 1.169 | 1.625 | 1.842 | 2.063 | 2.367 | 2.822 | 4.350 | 6.424 |
| 10 | | 0.009 | 0.026 | 0.094 | 0.163 | 0.258 | 0.383 | 0.455 | 0.847 | 1.057 | 1.470 | 1.666 | 1.866 | 2.141 | 2.553 | 3.935 | 5.812 |
| 15 | | 0.009 | 0.026 | 0.094 | 0.163 | 0.258 | 0.384 | 0.456 | 0.848 | 1.059 | 1.472 | 1.668 | 1.869 | 2.144 | 2.556 | 3.940 | 5.819 |
| 20 | | 0.009 | 0.025 | 0.091 | 0.156 | 0.248 | 0.368 | 0.437 | 0.813 | 1.015 | 1.411 | 1.600 | 1.792 | 2.056 | 2.451 | 3.779 | 5.580 |
| 25 | | 0.009 | 0.026 | 0.092 | 0.160 | 0.253 | 0.376 | 0.446 | 0.830 | 1.036 | 1.440 | 1.633 | 1.829 | 2.098 | 2.502 | 3.857 | 5.695 |
| 95 Percentile | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | | 0.093 | 0.269 | 0.968 | 1.670 | 2.646 | 3.933 | 4.671 | 8.690 | 10.848 | 15.077 | 17.090 | 19.147 | 21.962 | 26.187 | 40.371 | 59.617 |
| 3 | | 0.023 | 0.066 | 0.239 | 0.413 | 0.654 | 0.972 | 1.154 | 2.147 | 2.680 | 3.724 | 4.222 | 4.730 | 5.425 | 6.469 | 9.973 | 14.727 |
| 5 | | 0.018 | 0.051 | 0.184 | 0.318 | 0.505 | 0.750 | 0.891 | 1.657 | 2.068 | 2.874 | 3.258 | 3.650 | 4.187 | 4.992 | 7.696 | 11.366 |
| 10 | | 0.014 | 0.040 | 0.146 | 0.252 | 0.399 | 0.592 | 0.704 | 1.309 | 1.634 | 2.271 | 2.574 | 2.884 | 3.308 | 3.944 | 6.080 | 8.979 |
| 15 | | 0.013 | 0.037 | 0.134 | 0.231 | 0.365 | 0.543 | 0.645 | 1.200 | 1.498 | 2.082 | 2.360 | 2.644 | 3.033 | 3.616 | 5.575 | 8.233 |
| 20 | | 0.012 | 0.033 | 0.120 | 0.207 | 0.328 | 0.487 | 0.579 | 1.076 | 1.344 | 1.867 | 2.117 | 2.371 | 2.720 | 3.243 | 5.000 | 7.384 |
| 25 | | 0.012 | 0.033 | 0.120 | 0.207 | 0.328 | 0.487 | 0.578 | 1.076 | 1.343 | 1.867 | 2.116 | 2.370 | 2.719 | 3.242 | 4.998 | 7.381 |

Table F-3a (Also Table D.1-5). Frequentist Approach: Emissions Factor Uncertainty Ratios by Number of Tests (n) and Target Statistic: Wood Residue Combustion, Carbon Monoxide, Uncontrolled

| | | Target Statistic | | | | | | | | | | | | | | |
|----------------------|---------|------------------|--------------|---------------|---------------|---------------|---------------|--------|--------|---------------|---------------|---------------|---------------|---------------|---------------|---------|
| Median | | | | | | | | | | | | | | | | |
| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| 1 | 0.0020 | 0.0648 | 0.1855 | 0.2979 | 0.3915 | 0.4806 | 0.5754 | 1.0167 | 1.1640 | 1.6150 | 1.7677 | 1.9581 | 2.2158 | 2.6645 | 3.4704 | 5.1752 |
| 3 | 0.0018 | 0.0576 | 0.1651 | 0.2652 | 0.3485 | 0.4278 | 0.5122 | 0.9050 | 1.0362 | 1.4376 | 1.5736 | 1.7431 | 1.9725 | 2.3719 | 3.0893 | 4.6068 |
| 5 | 0.0018 | 0.0566 | 0.1622 | 0.2605 | 0.3423 | 0.4202 | 0.5031 | 0.8889 | 1.0177 | 1.4120 | 1.5455 | 1.7120 | 1.9373 | 2.3296 | 3.0342 | 4.5247 |
| 10 | 0.0018 | 0.0561 | 0.1608 | 0.2582 | 0.3394 | 0.4166 | 0.4988 | 0.8813 | 1.0090 | 1.3999 | 1.5323 | 1.6974 | 1.9207 | 2.3097 | 3.0083 | 4.4860 |
| 15 | 0.0018 | 0.0560 | 0.1605 | 0.2577 | 0.3387 | 0.4157 | 0.4977 | 0.8794 | 1.0068 | 1.3969 | 1.5289 | 1.6937 | 1.9165 | 2.3046 | 3.0017 | 4.4762 |
| 20 | 0.0018 | 0.0561 | 0.1608 | 0.2581 | 0.3393 | 0.4164 | 0.4986 | 0.8810 | 1.0086 | 1.3994 | 1.5317 | 1.6967 | 1.9200 | 2.3088 | 3.0072 | 4.4843 |
| 25 | 0.0017 | 0.0558 | 0.1599 | 0.2567 | 0.3374 | 0.4141 | 0.4958 | 0.8762 | 1.0031 | 1.3918 | 1.5233 | 1.6874 | 1.9095 | 2.2962 | 2.9907 | 4.4598 |
| Mean | | | | | | | | | | | | | | | | |
| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| 1 | 0.0041 | 0.1304 | 0.3735 | 0.5998 | 0.7884 | 0.9676 | 1.1585 | 2.0470 | 2.3436 | 3.2517 | 3.5591 | 3.9425 | 4.4613 | 5.3648 | 6.9875 | 10.4198 |
| 3 | 0.0021 | 0.0660 | 0.1891 | 0.3036 | 0.3990 | 0.4898 | 0.5864 | 1.0362 | 1.1863 | 1.6459 | 1.8015 | 1.9956 | 2.2582 | 2.7155 | 3.5368 | 5.2742 |
| 5 | 0.0019 | 0.0612 | 0.1752 | 0.2813 | 0.3697 | 0.4538 | 0.5433 | 0.9601 | 1.0992 | 1.5251 | 1.6692 | 1.8491 | 2.0924 | 2.5161 | 3.2772 | 4.8870 |
| 10 | 0.0018 | 0.0582 | 0.1668 | 0.2678 | 0.3520 | 0.4320 | 0.5173 | 0.9140 | 1.0464 | 1.4519 | 1.5891 | 1.7603 | 1.9920 | 2.3954 | 3.1199 | 4.6525 |
| 15 | 0.0018 | 0.0573 | 0.1640 | 0.2634 | 0.3462 | 0.4249 | 0.5087 | 0.8989 | 1.0291 | 1.4279 | 1.5629 | 1.7312 | 1.9591 | 2.3558 | 3.0683 | 4.5755 |
| 20 | 0.0018 | 0.0572 | 0.1637 | 0.2629 | 0.3456 | 0.4241 | 0.5078 | 0.8973 | 1.0273 | 1.4254 | 1.5601 | 1.7282 | 1.9556 | 2.3517 | 3.0630 | 4.5676 |
| 25 | 0.0018 | 0.0564 | 0.1617 | 0.2597 | 0.3413 | 0.4189 | 0.5015 | 0.8862 | 1.0145 | 1.4076 | 1.5407 | 1.7067 | 1.9313 | 2.3224 | 3.0248 | 4.5107 |
| 95 Percentile | | | | | | | | | | | | | | | | |
| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| 1 | 0.0110 | 0.3502 | 1.0033 | 1.6112 | 2.1176 | 2.5990 | 3.1118 | 5.4985 | 6.2951 | 8.7341 | 9.5599 | 10.5898 | 11.9833 | 14.4100 | 18.7686 | 27.9881 |
| 3 | 0.0039 | 0.1261 | 0.3613 | 0.5802 | 0.7626 | 0.9360 | 1.1207 | 1.9802 | 2.2671 | 3.1455 | 3.4429 | 3.8138 | 4.3157 | 5.1897 | 6.7594 | 10.0797 |
| 5 | 0.0032 | 0.1014 | 0.2904 | 0.4663 | 0.6129 | 0.7522 | 0.9006 | 1.5914 | 1.8220 | 2.5279 | 2.7669 | 3.0650 | 3.4683 | 4.1706 | 5.4321 | 8.1005 |
| 10 | 0.0026 | 0.0829 | 0.2375 | 0.3814 | 0.5013 | 0.6153 | 0.7367 | 1.3017 | 1.4903 | 2.0677 | 2.2632 | 2.5070 | 2.8369 | 3.4114 | 4.4432 | 6.6258 |
| 15 | 0.0024 | 0.0759 | 0.2174 | 0.3490 | 0.4587 | 0.5630 | 0.6741 | 1.1912 | 1.3638 | 1.8922 | 2.0711 | 2.2942 | 2.5961 | 3.1218 | 4.0660 | 6.0634 |
| 20 | 0.0023 | 0.0731 | 0.2093 | 0.3361 | 0.4417 | 0.5422 | 0.6491 | 1.1470 | 1.3132 | 1.8220 | 1.9943 | 2.2091 | 2.4998 | 3.0060 | 3.9153 | 5.8386 |
| 25 | 0.0022 | 0.0700 | 0.2006 | 0.3220 | 0.4233 | 0.5195 | 0.6220 | 1.0991 | 1.2583 | 1.7458 | 1.9109 | 2.1167 | 2.3953 | 2.8803 | 3.7516 | 5.5944 |

Table F-4. Alternative (Bayesian) Approach: Emissions Factor Uncertainty Ratios by Number of Tests (n) and Target Statistic: Wood Residue Combustion, Nox

| | | Target Statistic | | | | | | | | | | | | | | | |
|----------------------|--------|------------------|--------------|--------------|---------------|---------------|---------------|---------------|--------|--------|---------------|---------------|---------------|---------------|---------------|---------------|---------|
| Median | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | 0.1706 | 0.3282 | 0.4411 | 0.5312 | 0.5980 | 0.6674 | 0.7253 | 1.0071 | 1.1425 | 1.4175 | 1.5457 | 1.6849 | 1.9248 | 2.2630 | 3.1109 | 6.0479 | |
| 3 | 0.1588 | 0.3054 | 0.4105 | 0.4944 | 0.5566 | 0.6211 | 0.6750 | 0.9373 | 1.0633 | 1.3192 | 1.4386 | 1.5681 | 1.7914 | 2.1062 | 2.8953 | 5.6287 | |
| 5 | 0.1528 | 0.2939 | 0.3951 | 0.4758 | 0.5356 | 0.5977 | 0.6496 | 0.9020 | 1.0233 | 1.2696 | 1.3844 | 1.5091 | 1.7239 | 2.0269 | 2.7862 | 5.4167 | |
| 10 | 0.1513 | 0.2912 | 0.3914 | 0.4713 | 0.5306 | 0.5921 | 0.6435 | 0.8936 | 1.0137 | 1.2577 | 1.3714 | 1.4949 | 1.7077 | 2.0079 | 2.7601 | 5.3660 | |
| 15 | 0.1504 | 0.2894 | 0.3890 | 0.4685 | 0.5274 | 0.5885 | 0.6396 | 0.8882 | 1.0075 | 1.2500 | 1.3631 | 1.4858 | 1.6973 | 1.9957 | 2.7433 | 5.3333 | |
| 20 | 0.1499 | 0.2884 | 0.3877 | 0.4669 | 0.5256 | 0.5865 | 0.6375 | 0.8852 | 1.0042 | 1.2458 | 1.3585 | 1.4809 | 1.6917 | 1.9890 | 2.7342 | 5.3155 | |
| 25 | 0.1502 | 0.2891 | 0.3885 | 0.4679 | 0.5267 | 0.5878 | 0.6388 | 0.8871 | 1.0063 | 1.2485 | 1.3615 | 1.4840 | 1.6953 | 1.9932 | 2.7400 | 5.3269 | |
| Mean | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | 0.1914 | 0.3683 | 0.4950 | 0.5962 | 0.6711 | 0.7489 | 0.8139 | 1.1302 | 1.2821 | 1.5907 | 1.7346 | 1.8908 | 2.1600 | 2.5396 | 3.4910 | 6.7869 | |
| 3 | 0.1654 | 0.3182 | 0.4278 | 0.5151 | 0.5799 | 0.6471 | 0.7033 | 0.9766 | 1.1079 | 1.3745 | 1.4989 | 1.6338 | 1.8664 | 2.1945 | 3.0166 | 5.8647 | |
| 5 | 0.1573 | 0.3027 | 0.4068 | 0.4899 | 0.5515 | 0.6154 | 0.6689 | 0.9288 | 1.0536 | 1.3072 | 1.4255 | 1.5538 | 1.7750 | 2.0870 | 2.8688 | 5.5773 | |
| 10 | 0.1540 | 0.2963 | 0.3983 | 0.4796 | 0.5399 | 0.6025 | 0.6548 | 0.9093 | 1.0315 | 1.2798 | 1.3956 | 1.5212 | 1.7378 | 2.0432 | 2.8087 | 5.4605 | |
| 15 | 0.1519 | 0.2923 | 0.3929 | 0.4732 | 0.5327 | 0.5944 | 0.6460 | 0.8971 | 1.0177 | 1.2626 | 1.3769 | 1.5008 | 1.7145 | 2.0158 | 2.7710 | 5.3871 | |
| 20 | 0.1511 | 0.2907 | 0.3908 | 0.4706 | 0.5297 | 0.5912 | 0.6425 | 0.8922 | 1.0121 | 1.2556 | 1.3692 | 1.4925 | 1.7050 | 2.0047 | 2.7557 | 5.3573 | |
| 25 | 0.1510 | 0.2906 | 0.3906 | 0.4704 | 0.5295 | 0.5909 | 0.6422 | 0.8917 | 1.0116 | 1.2551 | 1.3686 | 1.4918 | 1.7042 | 2.0037 | 2.7544 | 5.3549 | |
| 95 Percentile | | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
| n | | | | | | | | | | | | | | | | | |
| 1 | 0.3780 | 0.7273 | 0.9776 | 1.1773 | 1.3252 | 1.4790 | 1.6073 | 2.2319 | 2.5319 | 3.1413 | 3.4255 | 3.7339 | 4.2655 | 5.0151 | 6.8941 | 13.4028 | |
| 3 | 0.2551 | 0.4908 | 0.6597 | 0.7945 | 0.8943 | 0.9981 | 1.0847 | 1.5062 | 1.7086 | 2.1199 | 2.3117 | 2.5198 | 2.8785 | 3.3844 | 4.6524 | 9.0448 | |
| 5 | 0.2246 | 0.4322 | 0.5810 | 0.6997 | 0.7876 | 0.8789 | 0.9552 | 1.3264 | 1.5047 | 1.8669 | 2.0358 | 2.2190 | 2.5350 | 2.9805 | 4.0971 | 7.9652 | |
| 10 | 0.1993 | 0.3835 | 0.5155 | 0.6208 | 0.6988 | 0.7799 | 0.8476 | 1.1769 | 1.3351 | 1.6565 | 1.8063 | 1.9689 | 2.2493 | 2.6446 | 3.6354 | 7.0675 | |
| 15 | 0.1882 | 0.3621 | 0.4867 | 0.5862 | 0.6598 | 0.7364 | 0.8003 | 1.1113 | 1.2606 | 1.5641 | 1.7056 | 1.8591 | 2.1238 | 2.4971 | 3.4326 | 6.6733 | |
| 20 | 0.1826 | 0.3513 | 0.4721 | 0.5686 | 0.6400 | 0.7143 | 0.7763 | 1.0780 | 1.2228 | 1.5171 | 1.6544 | 1.8033 | 2.0601 | 2.4221 | 3.3296 | 6.4731 | |
| 25 | 0.1781 | 0.3427 | 0.4606 | 0.5547 | 0.6244 | 0.6968 | 0.7573 | 1.0516 | 1.1930 | 1.4801 | 1.6140 | 1.7593 | 2.0098 | 2.3630 | 3.2483 | 6.3150 | |

Table F-4a (Also Table D.1-11). Frequentist Approach: Emissions Factor Uncertainty Ratios by Number of Tests (n) and Target Statistic: Wood Residue Combustion, Nitrogen Oxides, Uncontrolled

Target Statistic

Median

| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
|----|---------|--------------|--------------|---------------|---------------|---------------|---------------|--------|--------|---------------|---------------|---------------|---------------|---------------|---------------|----------|
| 1 | 0.0156 | 0.0638 | 0.1306 | 0.2037 | 0.2765 | 0.3496 | 0.4334 | 1.0031 | 2.1625 | 2.3340 | 2.8737 | 3.6691 | 4.9234 | 7.6758 | 17.4401 | 177.5230 |
| 3 | 0.0104 | 0.0424 | 0.0868 | 0.1353 | 0.1837 | 0.2322 | 0.2879 | 0.6663 | 1.4365 | 1.5504 | 1.9090 | 2.4373 | 3.2705 | 5.0989 | 11.5850 | 117.9246 |
| 5 | 0.0093 | 0.0380 | 0.0778 | 0.1214 | 0.1647 | 0.2083 | 0.2582 | 0.5975 | 1.2882 | 1.3903 | 1.7118 | 2.1856 | 2.9328 | 4.5723 | 10.3887 | 105.7472 |
| 10 | 0.0083 | 0.0338 | 0.0692 | 0.1079 | 0.1464 | 0.1851 | 0.2295 | 0.5311 | 1.1451 | 1.2359 | 1.5217 | 1.9429 | 2.6070 | 4.0645 | 9.2348 | 94.0017 |
| 15 | 0.0081 | 0.0331 | 0.0678 | 0.1057 | 0.1435 | 0.1815 | 0.2249 | 0.5206 | 1.1224 | 1.2114 | 1.4916 | 1.9044 | 2.5554 | 3.9840 | 9.0520 | 92.1409 |
| 20 | 0.0079 | 0.0321 | 0.0657 | 0.1025 | 0.1391 | 0.1758 | 0.2180 | 0.5045 | 1.0877 | 1.1739 | 1.4454 | 1.8455 | 2.4763 | 3.8608 | 8.7720 | 89.2901 |
| 25 | 0.0078 | 0.0317 | 0.0650 | 0.1014 | 0.1377 | 0.1741 | 0.2158 | 0.4994 | 1.0767 | 1.1620 | 1.4308 | 1.8268 | 2.4512 | 3.8216 | 8.6830 | 88.3846 |

Mean

| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
|----|---------|--------------|--------------|---------------|---------------|---------------|---------------|--------|--------|---------------|---------------|---------------|---------------|---------------|---------------|----------|
| 1 | 0.0326 | 0.1329 | 0.2724 | 0.4248 | 0.5766 | 0.7290 | 0.9037 | 2.0916 | 4.5093 | 4.8667 | 5.9922 | 7.6507 | 10.2660 | 16.0053 | 36.3653 | 370.1642 |
| 3 | 0.0140 | 0.0572 | 0.1172 | 0.1828 | 0.2481 | 0.3137 | 0.3888 | 0.9000 | 1.9403 | 2.0941 | 2.5784 | 3.2921 | 4.4174 | 6.8870 | 15.6478 | 159.2796 |
| 5 | 0.0112 | 0.0458 | 0.0939 | 0.1465 | 0.1988 | 0.2514 | 0.3116 | 0.7213 | 1.5551 | 1.6783 | 2.0665 | 2.6385 | 3.5404 | 5.5196 | 12.5411 | 127.6562 |
| 10 | 0.0092 | 0.0375 | 0.0769 | 0.1199 | 0.1628 | 0.2058 | 0.2551 | 0.5905 | 1.2731 | 1.3740 | 1.6917 | 2.1599 | 2.8983 | 4.5186 | 10.2667 | 104.5047 |
| 15 | 0.0086 | 0.0351 | 0.0720 | 0.1123 | 0.1525 | 0.1927 | 0.2389 | 0.5530 | 1.1922 | 1.2868 | 1.5843 | 2.0229 | 2.7143 | 4.2318 | 9.6150 | 97.8717 |
| 20 | 0.0083 | 0.0337 | 0.0691 | 0.1078 | 0.1463 | 0.1850 | 0.2293 | 0.5308 | 1.1443 | 1.2350 | 1.5206 | 1.9415 | 2.6052 | 4.0616 | 9.2283 | 93.9353 |
| 25 | 0.0081 | 0.0329 | 0.0675 | 0.1052 | 0.1428 | 0.1806 | 0.2238 | 0.5180 | 1.1168 | 1.2053 | 1.4841 | 1.8949 | 2.5426 | 3.9641 | 9.0068 | 91.6802 |

95 Percentile

| n | Minimum | 1 Percentile | 5 Percentile | 10 Percentile | 15 Percentile | 20 Percentile | 25 Percentile | Median | Mean | 75 Percentile | 80 Percentile | 85 Percentile | 90 Percentile | 95 Percentile | 99 Percentile | Maximum |
|----|---------|--------------|--------------|---------------|---------------|---------------|---------------|--------|---------|---------------|---------------|---------------|---------------|---------------|---------------|-----------|
| 1 | 0.1204 | 0.4913 | 1.0067 | 1.5700 | 2.1310 | 2.6942 | 3.3398 | 7.7300 | 16.6651 | 17.9861 | 22.1459 | 28.2752 | 37.9408 | 59.1519 | 134.3979 | 1368.0411 |
| 3 | 0.0369 | 0.1506 | 0.3086 | 0.4812 | 0.6532 | 0.8258 | 1.0237 | 2.3693 | 5.1080 | 5.5129 | 6.7879 | 8.6666 | 11.6292 | 18.1306 | 41.1943 | 419.3185 |
| 5 | 0.0258 | 0.1052 | 0.2156 | 0.3363 | 0.4564 | 0.5770 | 0.7153 | 1.6555 | 3.5692 | 3.8521 | 4.7430 | 6.0557 | 8.1258 | 12.6686 | 28.7841 | 292.9942 |
| 10 | 0.0177 | 0.0723 | 0.1482 | 0.2311 | 0.3136 | 0.3965 | 0.4915 | 1.1377 | 2.4528 | 2.6472 | 3.2594 | 4.1615 | 5.5841 | 8.7059 | 19.7805 | 201.3467 |
| 15 | 0.0150 | 0.0614 | 0.1258 | 0.1962 | 0.2663 | 0.3367 | 0.4173 | 0.9659 | 2.0825 | 2.2475 | 2.7674 | 3.5333 | 4.7411 | 7.3916 | 16.7944 | 170.9507 |
| 20 | 0.0137 | 0.0561 | 0.1149 | 0.1792 | 0.2432 | 0.3075 | 0.3812 | 0.8824 | 1.9023 | 2.0531 | 2.5279 | 3.2275 | 4.3308 | 6.7520 | 15.3411 | 156.1575 |
| 25 | 0.0128 | 0.0524 | 0.1074 | 0.1675 | 0.2274 | 0.2875 | 0.3564 | 0.8249 | 1.7784 | 1.9193 | 2.3632 | 3.0173 | 4.0488 | 6.3122 | 14.3419 | 145.9872 |

F.2 Method for Computing Targeted Quantiles of Fitted Distributions

During the study, once the parametric distribution was chosen, the various quantiles of the distribution (ranging from 1st to 99th percentiles values) were estimated by simulating a sample size 10,000; ranking each value from smallest to biggest; and choosing the value corresponding to each percentile in the sample. One peer reviewer indicated that although this was a valid and accurate procedure for estimating the targeted quantiles, it was unnecessary. The reviewer indicated that the population quantiles could be calculated directly using an inverse cumulative distribution function (CDF) calculation. Although this is true, for the statistical design of this study, we needed the 10,000 population values to generate the sampling distributions of means for various values of n (where n is the number of tests comprising an emissions factor). Sampling distributions of means of varying n were produced to incorporate into the uncertainty ratios the effect (variability) resulting from varying values of n .

Based upon the reviewer's recommendation, we conducted an assessment of the uncertainty induced by the sampling error associated with the estimation of the quantiles of the hypothetical population using a sample of size 10,000 from the corresponding Weibull or log-normal distributions, as compared to using the corresponding inverse CDF calculation. The percentiles were calculated using an equation for the inverse CDF of the Weibull distribution implemented in Splus and an implementation of the CDF for the log-normal distribution available in Microsoft Office EXCEL as suggested by the reviewer. Quantile values corresponding to a sequence of probabilities from 0.05 to 0.95 were calculated using the inverse CDF for each of the 44 emissions factors considered. The inverse CDF quantiles values were compared to the values obtained using the hypothetical population of size 10,000 by subtraction. The log-normal and Weibull percentiles derived from the population values showed a maximum difference from the inverse CDF values of 0.01. Uncertainty ratio values were then calculated for selected emissions factors using the inverse CDF quantiles and compared to the proposed study uncertainty ratios. Results show no significant difference between the two values obtained for the uncertainty. The comparison results (or deltas) are presented in Tables F-5 and F-6; these tables contain the difference between the quantiles based on the sample of size 10,000 (from the study) and the CDF equations for the Weibull and log-normal densities, respectively.

Table F-5. Difference in Quantiles Based Upon Sample of 10,000 and Inverse CDF Calculation for Weibull

| Quantiles | Arsenic, Wood Comb. | Cadmium, Wood Comb. | Carbon Monoxide, Wood Comb. | Chromium, Wood Comb. | HCl, UNC, Rrefuse Comb. | HCl, SD/FF, Refuse Comb. | Lead, Wood Comb. | Mercury, Wood Comb. | Nickel, Wood Comb. | Nitrogen Oxides | PM- cond.- organic, Asphalt- Batch | PM- filterable, DSI/FF, Refuse comb. | PM- filterable, WS, Wood Comb. | PM- filterable, MC, Wood comb. | Sulfur dioxide, refuse Comb. |
|-----------|---------------------------|---------------------------|--------------------------------------|----------------------------|----------------------------------|-----------------------------------|------------------------|---------------------------|--------------------------|--------------------|--|--|--|--|---------------------------------------|
| 0.05 | 0.0000 | 0.0000 | -0.0021 | 0.0000 | -0.0306 | 0.0003 | 0.0000 | 0.0000 | 0.0000 | -0.0044 | 0.0000 | 0.0000 | 0.0003 | 0.0000 | -0.0346 |
| 0.10 | 0.0000 | 0.0000 | 0.0009 | 0.0000 | 0.0199 | 0.0006 | 0.0000 | 0.0000 | 0.0000 | 0.0050 | 0.0000 | 0.0005 | -0.0001 | -0.0002 | -0.0178 |
| 0.15 | 0.0000 | 0.0000 | 0.0011 | 0.0000 | 0.0232 | 0.0005 | 0.0000 | 0.0000 | 0.0000 | 0.0058 | 0.0000 | -0.0003 | 0.0001 | -0.0007 | -0.0158 |
| 0.20 | 0.0000 | 0.0000 | -0.0001 | 0.0000 | 0.0475 | 0.0013 | 0.0000 | 0.0000 | 0.0000 | -0.0065 | 0.0000 | -0.0009 | -0.0001 | -0.0007 | -0.0267 |
| 0.25 | 0.0000 | 0.0000 | -0.0001 | 0.0000 | 0.0483 | 0.0010 | 0.0000 | 0.0000 | 0.0000 | -0.0126 | 0.0000 | -0.0012 | -0.0002 | -0.0001 | -0.0069 |
| 0.30 | 0.0000 | 0.0000 | 0.0021 | 0.0000 | 0.0303 | 0.0009 | 0.0000 | 0.0000 | 0.0000 | -0.0127 | 0.0000 | -0.0012 | -0.0004 | 0.0011 | -0.0018 |
| 0.35 | 0.0000 | 0.0000 | 0.0030 | 0.0000 | 0.0106 | 0.0008 | 0.0000 | 0.0000 | 0.0000 | -0.0120 | 0.0000 | -0.0002 | -0.0003 | 0.0017 | -0.0152 |
| 0.40 | 0.0000 | 0.0000 | -0.0003 | 0.0000 | 0.0097 | 0.0010 | 0.0000 | 0.0000 | 0.0000 | -0.0130 | 0.0000 | -0.0014 | -0.0004 | 0.0025 | -0.0263 |
| 0.45 | 0.0000 | 0.0000 | 0.0010 | 0.0000 | -0.0214 | 0.0018 | 0.0000 | 0.0000 | 0.0000 | -0.0170 | 0.0000 | -0.0002 | -0.0004 | 0.0028 | -0.0207 |
| 0.50 | 0.0000 | 0.0000 | 0.0002 | 0.0000 | -0.0554 | 0.0008 | 0.0000 | 0.0000 | 0.0000 | -0.0215 | 0.0000 | -0.0003 | -0.0005 | 0.0020 | -0.0136 |
| 0.55 | 0.0000 | 0.0000 | 0.0002 | 0.0000 | -0.0610 | 0.0020 | 0.0000 | 0.0000 | 0.0000 | -0.0109 | 0.0000 | 0.0006 | -0.0004 | 0.0019 | -0.0127 |
| 0.60 | 0.0000 | 0.0000 | 0.0001 | 0.0000 | -0.0557 | 0.0005 | 0.0000 | 0.0000 | 0.0000 | -0.0206 | 0.0000 | -0.0002 | -0.0004 | 0.0033 | -0.0121 |
| 0.65 | 0.0000 | 0.0000 | -0.0018 | 0.0000 | -0.0668 | 0.0006 | 0.0000 | 0.0000 | 0.0000 | -0.0105 | 0.0000 | 0.0008 | -0.0002 | 0.0047 | -0.0011 |
| 0.70 | 0.0000 | 0.0000 | -0.0074 | 0.0000 | -0.0885 | -0.0001 | 0.0000 | 0.0000 | 0.0000 | -0.0080 | 0.0000 | 0.0011 | -0.0002 | 0.0051 | -0.0137 |
| 0.75 | 0.0000 | 0.0000 | -0.0034 | 0.0000 | -0.0854 | -0.0006 | 0.0000 | 0.0000 | 0.0000 | -0.0049 | 0.0000 | 0.0019 | -0.0002 | 0.0060 | 0.0008 |
| 0.80 | 0.0000 | 0.0000 | -0.0118 | 0.0000 | -0.0437 | 0.0014 | 0.0000 | 0.0000 | 0.0000 | -0.0033 | 0.0000 | -0.0012 | -0.0001 | 0.0061 | -0.0039 |
| 0.85 | 0.0000 | 0.0000 | -0.0194 | 0.0000 | -0.0349 | -0.0010 | 0.0000 | 0.0000 | 0.0000 | -0.0073 | 0.0000 | -0.0030 | -0.0003 | 0.0052 | 0.0030 |
| 0.90 | 0.0000 | 0.0000 | -0.0155 | 0.0000 | -0.0113 | 0.0036 | 0.0000 | 0.0000 | 0.0000 | -0.0160 | 0.0000 | -0.0025 | -0.0003 | 0.0039 | 0.0202 |
| 0.95 | 0.0000 | 0.0000 | -0.0294 | 0.0000 | -0.0144 | -0.0163 | 0.0000 | 0.0000 | 0.0000 | -0.0328 | 0.0000 | -0.0017 | 0.0001 | 0.0195 | -0.0521 |

Table F-6. Difference in Quantiles Based Upon Sample of 10,000 and Inverse CDF Calculation for Log-normal

| Quantiles | Acetaldehyde, Wood Comb. | Arsenic, Refuse Comb | Benzene, Asphalt- Drum | Benzene, Wood Comb. | Cadmium, SD ESP, Refuse Comb. | Carbon Monoxide, Refuse Comb. | Formaldehyde, Asphalt-Drum | Formaldehyde, Wood Comb. | Lead, SD/ESP Refuse Comb. | Mercury, SD/FF Refuse Comb. | Nickel SD/FF Refuse Comb. | Nitrogen Oxides, Wood Comb. | PM-cond., Wood Comb. | PM-cond., inorganic Asphalt |
|-----------|-----------------------------|----------------------------|------------------------------|---------------------------|--|--|-------------------------------|-----------------------------|------------------------------------|--------------------------------------|------------------------------------|--------------------------------------|----------------------------|-----------------------------------|
| 0.05 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0026 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0011 | 0.0000 | 0.0000 |
| 0.10 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0014 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0011 | 0.0000 | 0.0000 |
| 0.15 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0024 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0011 | 0.0000 | 0.0000 |
| 0.20 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0007 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0013 | 0.0000 | 0.0000 |
| 0.25 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0005 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0021 | 0.0000 | 0.0000 |
| 0.30 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0003 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0028 | 0.0000 | 0.0000 |
| 0.35 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0012 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0013 | 0.0000 | 0.0000 |
| 0.40 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0008 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0022 | 0.0000 | -0.0001 |
| 0.45 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0006 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0028 | 0.0000 | -0.0001 |
| 0.50 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0002 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0030 | 0.0001 | -0.0001 |
| 0.55 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0012 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0037 | 0.0001 | -0.0001 |
| 0.60 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0026 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0044 | 0.0001 | 0.0000 |
| 0.65 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0053 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0047 | 0.0003 | 0.0001 |
| 0.70 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0047 | 0.0000 | 0.0001 | 0.0000 | 0.0000 | 0.0000 | -0.0082 | 0.0004 | 0.0001 |
| 0.75 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0033 | 0.0000 | 0.0001 | 0.0000 | 0.0000 | 0.0000 | -0.0094 | 0.0004 | 0.0002 |
| 0.80 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0061 | 0.0000 | 0.0001 | 0.0000 | -0.0001 | 0.0000 | -0.0094 | 0.0002 | 0.0003 |
| 0.85 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0173 | 0.0000 | 0.0001 | 0.0000 | -0.0001 | 0.0000 | -0.0057 | 0.0003 | 0.0004 |
| 0.90 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0246 | 0.0000 | 0.0002 | 0.0000 | -0.0001 | 0.0000 | -0.0001 | 0.0000 | 0.0003 |
| 0.95 | 0.0001 | 0.0000 | 0.0000 | -0.0001 | 0.0000 | 0.0212 | 0.0001 | 0.0006 | -0.0001 | -0.0001 | 0.0000 | -0.0052 | 0.0003 | 0.0014 |

Table F-6 continued.

| Quantiles | PM-cond., inorganic, WS/FF Asphalt | PM-cond., organic WS/FF Asphalt | PM- filterable Asphalt, Batch Mix | PM- filterable Asphalt, Drum Mix | PM- filterable OSB, Hot Press | PM- filterable, ESP, Refuse Comb. | PM- filterable, SD/ ESP Refuse Comb. | PM- filterable SD/FF Refuse Comb. | PM- filterable, UNC, Refuse Comb. | PM- filterable, ESP, Refuse Comb. | PM- filterable, UNC, Refuse Comb. | PM- filterable, MC, Wood Comb. | PM- filterable, UNC, Wood Comb. | PM- filterable, UNC, Wood Comb. | Sulfur dioxide, Wood Comb. |
|-----------|---|--|--|---|--|---|--|---|---|---|---|---|--|--|-------------------------------------|
| 0.05 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0005 | 0.0002 | 0.0000 | 0.0002 | 0.0234 | -0.0010 | -0.0374 | -0.0010 | 0.0018 | -0.0004 | 0.0000 |
| 0.10 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0007 | 0.0004 | 0.0000 | 0.0001 | 0.0632 | 0.0003 | 0.0224 | 0.0004 | 0.0020 | -0.0002 | 0.0000 |
| 0.15 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | -0.0001 | 0.0005 | -0.0003 | -0.0003 | 0.0683 | -0.0001 | 0.0045 | 0.0011 | -0.0006 | 0.0012 | 0.0000 |
| 0.20 | 0.0000 | 0.0000 | 0.0001 | 0.0000 | 0.0003 | 0.0000 | 0.0000 | -0.0003 | -0.0043 | -0.0009 | 0.0152 | 0.0013 | -0.0003 | 0.0012 | 0.0000 |
| 0.25 | 0.0000 | 0.0000 | 0.0001 | -0.0001 | 0.0002 | 0.0008 | -0.0002 | -0.0002 | 0.0224 | -0.0028 | 0.0196 | 0.0012 | 0.0016 | 0.0002 | 0.0000 |
| 0.30 | 0.0000 | 0.0000 | 0.0002 | -0.0001 | 0.0008 | 0.0011 | -0.0004 | -0.0002 | -0.0863 | -0.0018 | 0.0155 | 0.0016 | 0.0016 | 0.0011 | 0.0000 |
| 0.35 | 0.0000 | 0.0000 | 0.0002 | 0.0000 | 0.0004 | 0.0016 | -0.0002 | -0.0004 | -0.0641 | -0.0037 | 0.0304 | 0.0007 | 0.0010 | 0.0002 | 0.0000 |
| 0.40 | 0.0001 | 0.0001 | 0.0002 | -0.0001 | 0.0002 | 0.0019 | -0.0003 | -0.0002 | -0.0895 | -0.0050 | 0.0288 | 0.0008 | 0.0013 | -0.0001 | 0.0000 |
| 0.45 | 0.0001 | 0.0001 | 0.0001 | -0.0001 | 0.0004 | 0.0015 | -0.0004 | -0.0003 | -0.0734 | -0.0028 | 0.0294 | 0.0022 | 0.0002 | -0.0021 | 0.0000 |
| 0.50 | 0.0001 | 0.0001 | 0.0000 | -0.0001 | 0.0006 | 0.0011 | -0.0004 | 0.0001 | -0.0550 | -0.0033 | 0.0319 | 0.0020 | -0.0003 | -0.0005 | 0.0000 |
| 0.55 | 0.0001 | 0.0000 | 0.0000 | 0.0000 | 0.0004 | 0.0006 | -0.0003 | -0.0002 | -0.0963 | -0.0052 | 0.0330 | 0.0018 | 0.0013 | -0.0027 | 0.0001 |
| 0.60 | 0.0001 | 0.0000 | 0.0001 | -0.0001 | -0.0002 | -0.0003 | 0.0001 | 0.0000 | -0.0959 | -0.0019 | 0.0435 | 0.0020 | -0.0001 | -0.0021 | 0.0002 |
| 0.65 | 0.0001 | 0.0001 | -0.0001 | 0.0000 | 0.0010 | -0.0007 | 0.0002 | 0.0000 | -0.0274 | -0.0012 | 0.0539 | 0.0032 | 0.0016 | -0.0056 | 0.0002 |
| 0.70 | 0.0000 | -0.0001 | 0.0000 | 0.0000 | 0.0007 | -0.0004 | -0.0003 | -0.0003 | -0.0174 | -0.0042 | 0.0630 | 0.0014 | -0.0022 | -0.0034 | 0.0005 |
| 0.75 | 0.0000 | -0.0002 | -0.0003 | 0.0001 | 0.0005 | 0.0017 | -0.0004 | -0.0009 | -0.0801 | 0.0032 | 0.0518 | 0.0017 | 0.0013 | -0.0017 | 0.0003 |
| 0.80 | 0.0000 | -0.0004 | -0.0004 | -0.0001 | 0.0025 | -0.0006 | -0.0001 | -0.0012 | -0.0730 | -0.0008 | 0.0718 | 0.0012 | 0.0001 | -0.0067 | 0.0005 |
| 0.85 | 0.0000 | -0.0006 | -0.0004 | -0.0002 | -0.0045 | -0.0055 | -0.0002 | -0.0018 | 0.0050 | -0.0176 | 0.0641 | -0.0071 | 0.0021 | -0.0014 | 0.0005 |
| 0.90 | 0.0001 | -0.0008 | 0.0014 | -0.0006 | -0.0089 | -0.0041 | 0.0003 | -0.0036 | 0.0161 | 0.0109 | 0.0482 | -0.0077 | 0.0084 | 0.0054 | 0.0007 |
| 0.95 | -0.0002 | -0.0003 | 0.0003 | -0.0008 | -0.0099 | -0.0178 | 0.0011 | -0.0076 | -0.0414 | -0.0212 | 0.0503 | -0.0059 | 0.0120 | 0.0060 | 0.0006 |